

This document gives full references to the papers cited in the slides for Robert Holte's AAAI 2005 tutorial "Where Do Heuristics Come From ? (The Use of Abstraction to Speed Up Search)", plus a few extra references.

The list below follows exactly the same order as the slides.

## 1 PART 1

General introduction to search: [73].

Dijkstra's algorithm: [13].

A\*: [29].

IDA\*: [46].

Breadth-first Heuristic Search: [79].

Algorithm "C": [2].

Limited Discrepancy Search: [30].

RBFS: [48].

SMA\*: [72].

Weighted A\*: [67].

RTA\*: [47].

BULB (Beam search with limited discrepancy backtracking): [24].

ABSTRIPS: [74].

ALPINE: [45].

Bacchus and Yang: [1].

Refinement Search for Explicit Graphs: [37].

Reinforcement Learning: [76].

Learning Heuristics: [18].

Speedup Learning for planning: [23,78,81].

Lookahead search: [4,5,47].

Metalevel Reasoning: [8].

GPS (the General Problem Solver): [65].

Multi-Tac: [62].

Puzzles - solving Rubik's Cube optimally: [49].

Parsing: [44].

Dynamic Programming - State Space Relaxation (SSR): [7].

Coarse-to-Fine Dynamic Programming - CFDP: [69].

Weighted logic programs: [22].

Quality-of-Service Routing in Networks: [57].

Sequential Ordering Problem: [34].  
Co-operative Pathfinding: [75].  
Vertex Cover: [19].  
Multiple Sequence Alignment: [55,60,80].  
Building Macro-Tables with optimal entries: [33].  
Planning: [3,17,31].  
Constrained Optimization (Mini-bucket elimination): [43].

Branch-and-bound: [9,16,71].  
The Graph Traverser: [15].  
A\*: [29].

Minsky's early description of refinement: [61].  
ABSTRIPS: [74].  
Somalvico and colleagues: [27,58].  
Gaschnig: [25].  
Valtorta: [77].  
Pearl: [66].  
ABSOLVER: [63,68].  
Multi-level version of Valtorta's theorem: [28].

Using memory to speed up search.  
IDA\*: [46].  
MA\*: [6].  
IE, SMA\*: [72].  
Perimeter Search: [14,59].  
ITS: [26].  
Memory Enhanced IDA\* (transposition tables): [70].

Pattern Databases: [10–12].  
Hierarchical Heuristic Search (Hierarchical A\*): [39,38].

## 2 PART 2

General definitions of domain abstraction and several basic results, including “size matters” and non-surjective abstractions: [32,35,36,41].

Korf and Reid formula for using the distribution of heuristic values to predict search performance: [54,53,41].

Pattern Databases: [10–12].  
Hierarchical A\* (HA\*): [38].  
Hierarchical IDA\* (HIDA\*): [40].

Delayed Duplicate Detection (DDD): [50,51].  
Frontier Search: [55].

Efficient perfect hash functions for permutations: [64,56].

Optimal path caching and P-g caching: [38].

### 3 PART 3

Max'ing: [42].  
Pattern Database Compression: [20].  
Dovetailing: [10–12].

Additive Pattern Databases: [19,52].  
Max'ing after adding: [42].

Space efficient pattern databases: [80].  
Hierarchical IDA\*: [40].  
Reverse Resumable A\*: [75].

Super-customization: [19,34,35].

Multiple PDB lookups based on symmetries: [10–12].  
“Dual” PDB lookups: [21].

Coarse-to-Fine Dynamic Programming - CFDP: [69].

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