

## 14. Sampling

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## Imperfect Information

- What do you do when you have imperfect information?
- Poker [1], bridge [2] (don't know the opponent's cards)
- Scrabble [3] (don't know the opponent's tiles)
- Regular search gives rise to too many possibilities

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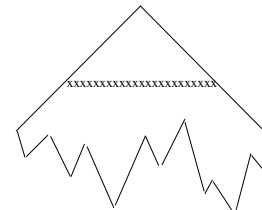
## Choices?

- Alpha-beta? Don't know what moves the opponent might have.
- \*-Minimax? Could have a large branching factor, meaning little search depth
- How do you get meaningful results when there can be stochastic events and hidden information?

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## Traditional Search



All nodes at a fixed search depth.

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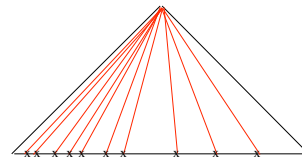
## Solution?

- Sample from the space of possibilities!
- If you get “enough” samples, then you may have a good approximation to the real value.

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## Sampling Search



Some nodes at a deep search depth.

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## 1. Sample

- Construct a plausible scenario from the current state to a desirable (possibly goal) state
- Compute the value of this sequence of moves
- E.g. in poker, compute a plausible sequence of actions from the current state to the end of the game

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## 2. Statistical Sampling

- For each move choice at the root node
  - Gather samples
  - Compute performance metric (e.g. average score achieved)
- Repeat until resources are exhausted (usually time)

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### 3. Choose Action

- Choose move with the best statistical outcome
- Poker: betting choice leading to best average winnings
- Scrabble: move that leads to best average number of points
- Bridge: move that leads to the most tricks won on average

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### How Many Samples?

- Iterate until time runs out
- Iterate until statistically confident
- Iterate until one move choice is significantly better than the alternatives
- Smart sampling can be used to help reduce the number of samples needed to converge to a useful result [4]

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### Selective Sampling

- Don't want random sequences
- Need to bias play along lines likely to occur
- All scenarios are not equal; use all available information to bias the sampling in proportion to likely scenarios
- E.g. Bridge: bias play to be consistent with the bidding

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### Advantages of Sampling

- Simple search algorithm!
- Can realize complex behaviors with no explicit knowledge
- Lessens dependence on expert knowledge

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## Disadvantages of Sampling

- May not converge to a clear “winner”
- To get useful results may need to include “opponent modeling”
  - Observe opponent to determine their likely move choices
  - Opponent modeling is a hard problem!

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## Results?

- Improved play in poker
- World championship caliber play in Scrabble
- Strong play in bridge
- Also used in backgammon to compute expected outcomes (rollouts)

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## Monte Carlo...or...Alpha-Beta?

- Statistical sampling has been used as a replacement for alpha-beta search in computer Go.
- Play sequences of Go moves and then compute the value at the end of the line
- Enhance sampling to rule out “weak” moves
- Plays at a reasonable level of play!

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## References (incomplete)

- 1) D. Billings et al, AAAI, 1999, see me.
- 2) M. Ginsberg, IJCAI 1999.
- 3) B. Sheppard, “Towards Perfect Play at Scrabble”, Ph.D. thesis, 2002.
- 4) B. Sheppard, ICGA Journal, 2004.
- 5) B. Bouzy, “Monte Carlo Go”, 2003.

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