Lecture 4 Week 5 (April 7) and Week 6 (April 14)

33459-01 Principles of Knowledge Discovery in Data

Classification: Neural Networks, Naïve Bayesian Classification, k-Nearest Neighbors, Decision Trees & Associative Classifiers

Lecture by: Dr. Osmar R. Zaïane

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Course Content

- Introduction to Data Mining
- Association analysis
- Sequential Pattern Analysis
- Classification and prediction
- Contrast Sets
- Data Clustering
- Outlier Detection
- Web Mining

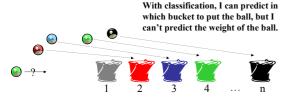
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What is Classification?

The goal of data classification is to organize and categorize data in distinct classes.

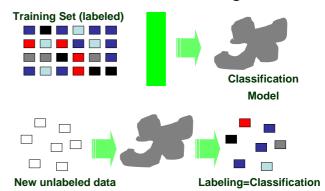
- ▶ A model is first created based on the data distribution.
- ▶ The model is then used to classify new data.
- ▶ Given the model, a class can be predicted for new data.



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Classification = Learning a Model



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Classification is a three-step process

1. Model construction (Learning):

- Each tuple is assumed to belong to a predefined class, as determined by one of the attributes, called the class label.
- The set of all tuples used for construction of the model is called training set.
- The model is represented in the following forms:
 - · Classification rules, (IF-THEN statements),
 - Decision tree
 - Mathematical formulae

Classification is a three-step process

2. Model Evaluation (Accuracy):

Estimate accuracy rate of the model based on a test set.

- The known label of test sample is compared with the classified result from the model.
- Accuracy rate is the percentage of test set samples that are correctly classified by the model.
- Test set is independent of training set otherwise overfitting will occur.

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Classification is a three-step process

3. Model Use (Classification):

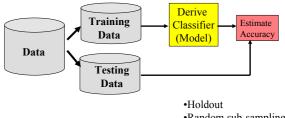
The model is used to classify unseen objects.

- Give a class label to a new tuple
- Predict the value of an actual attribute

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Classification with Holdout



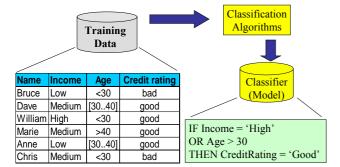
- •Random sub-sampling
- •K-fold cross validation
- •Bootstrapping

• ...

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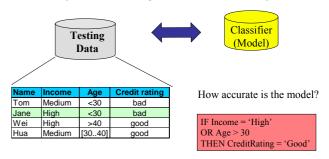
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1. Classification Process (Learning)



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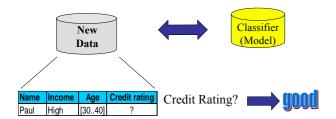
2. Classification Process (Accuracy Evaluation)



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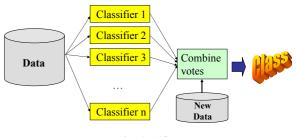
3. Classification Process (Classification)



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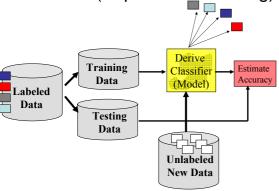
Improving Accuracy



Composite classifier

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Framework (Supervised Learning)



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(1 hour)

Classification Methods

Decision Tree Induction Neural Networks

❖ Bayesian Classification Tool

Associative Classifiers

* K-Nearest Neighbour Next week Support Vector Machines

Case-Based Reasoning

Genetic Algorithms

* Rough Set Theory

Fuzzy Sets

. Etc.

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Lecture Outline

Part I: Artificial Neural Networks (ANN)

- Introduction to Neural Networks
 - Biological Neural System
 - What is an artificial neural network?
 - Neuron model and activation function
 - Construction of a neural network
 - Learning: Backpropagation Algorithm
 - Forward propagation of signal
 - Backward propagation of error
 - Example

Part II: Bayesian Classifiers (Statistical-based) (1 hour)

- What is Bayesian Classification
- Bayes theorem
- Naïve Bayes Algorithm
 - Using Laplace Estimate
- Handling Missing Values and Numerical Data
- Belief Networks

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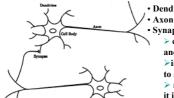
Human Nervous System

- We have only just began to understand how our neural system operates
- A huge number of neurons and interconnections between them
 - 100 billion (i.e. 1010) neurons in the brain
 - a full Olympic-sized swimming pool contains 1010 raindrops; the number of stars in the Milky Way is of the same magnitude
 - 104 connections per neuron
- Biological neurons are slower than computers
 - Neurons operate in 10⁻³ seconds, computers in 10⁻⁹ seconds
 - The brain makes up for the slow rate of operation by a single neurone by the large number of neurons and connections (think about the speed of face recognition by a human, for example, and the time it takes fast computers to do the same task.)

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Biological Neurons

- The purpose of neurons: transmit information in the form of electrical signals
 - it accepts many inputs, which are all added up in some way
 - if enough active inputs are received at once, the neuron will be activated and fire; if not, it remain in its inactive state
- Structure of neuron · Cell body contains nucleus holding the chromosomes



Dendrites

Synapse couples the axon with the dendrite of another cell;

>information is passed from one neuron to another through synapses;

no direct linkage across the junction,

it is a chemical one.

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Operation of biological neurons

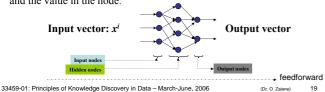
- Signals are transmitted between neurons by electrical pulses (action potentials, AP) traveling along the axon;
- When the potential at the synapse is raised sufficiently by the AP, it releases chemicals called neurotransmitters
 - it may take the arrival of more than one AP before the synapse is triggered
- The neurotransmitters diffuse across the gap and chemically activate gates on the dendrites, that allows charged ions to flow
- The flow of ions alters the potential of the dendrite and provides a voltage pulse on the dendrite (post-synaptic-potential, PSP)
 - some synapses excite the dendrite they affect, while others inhibit it
 - the synapses also determine the strength of the new input signal
- Each PSP travels along its dendrite and spreads over the soma (cell body)
- The soma sums the effects of thousands PSPs; if the resulting potential exceeds a threshold, the neuron fires and generates another AP.

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What is an Artificial Neural Network (NN)?

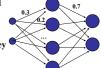
A neural network is a data structure that supposedly simulates the behaviour of neurons in a biological brain.

A neural network is composed of layers of units interconnected. Messages are passed along the connections from one unit to the other. Messages can change based on the *weight* of the connection and the value in the node.



What is an Artificial Neural Network (NN)?

- A network of many simple *units* (neurons, nodes)
 - The units are connected by connections.
 - Each connection has a numeric weight associated with it.
 - Units receive inputs (from the environment or other units) via the connections. They produce output using their weights and the inputs (i.e. they operate locally).

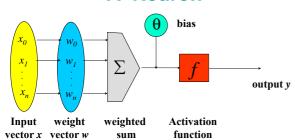


- A NN can be represented as a directed graph.
- NNs *learn from examples* and exhibit some capability for generalization beyond the training data.
 - knowledge is acquired by the network from its environment via learning and is stored in the weights of the connections.
 - the training (learning) rule a procedure for modifying the weights of connections in order to perform a certain task.
 - There are also some sophisticated techniques that allow learning by adding and pruning connections (between nodes).

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A Neuron



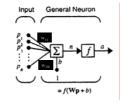
• The *n*-dimensional input vector *x* is mapped into variable *y* by means of the scalar product and a nonlinear function mapping.

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Neuron Model

- Each connection from unit i to j has a numeric weigh w_{ij} associated with it, which determines the strength and the sign of the connection
- Each neuron first computes the weighed sum of its inputs w, and then applies an activation function f to derive the output (activation) a
- A neuron may have a special weight called bias weight b. It is connected to a fixed input of 1.
- NNs represent a function of their weights (parameters). By adjusting the weights, we change this function. This is done by using a learning rule.



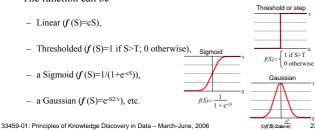
if there are 2 inputs $p_1=2$ and $p_2=3$, and if $w_{11}=3$, $w_{12}=1$, b=-1.5, then $a=f(2^*3+3^*1-1.5)=f(7.5)$ $f(P_1^*w_{11}+P_2^*w_{12}+b)$ What is:

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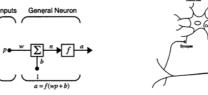
Activation function

- Activation function, processing element, squashing function, firing rule...
- Is applied by each neuron to its input values and weights (as well as the bias) $S_i = \theta_i + \Sigma_{i=1..n} (x_{ij} * W_{ij})$
- Can be unipolar [0,1] bipolar [-1, 1]
- The function can be



Correspondence Between Artificial and Biological Neurons

- How this artificial neuron relates to the biological one?
 - input p (or input vector p) input signal (or signals) at the dendrite
 - weight w (or weight vector w) strength of the synapse (or synapses)
 - summer & transfer function cell body
 - neuron output a signal at the axon



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Constructing the Network

- · The number of input nodes: Generally corresponds to the dimensionality of the input tuples. Input is converted into binary and concatenated to form and bitstream.
 - Eg. age 20-80: 6 intervals
 - [20, 30) \rightarrow 000001, [30, 40) \rightarrow 000010,, [70, 80) \rightarrow 100000
 - $[20, 30) \rightarrow 001, [30, 40) \rightarrow 010, ..., [70, 80) \rightarrow 110$
- · Number of hidden nodes: Determined by expert, or in some cases, adjusted during training.
- Number of output nodes: Generally number of classes
 - Eq. 10 classes
 - 0000000001 \rightarrow C1, 0000000010 \rightarrow C2,, 1000000000 \rightarrow C10
 - 0001 \rightarrow C1, 0010 \rightarrow C2,, 1010 \rightarrow C10

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Neural Networks - Pros and Cons

Advantages

- prediction accuracy is generally high.
- robust, works when training examples contain errors.
- output may be discrete, real-valued, or a vector of several discrete or real-valued attributes.
- fast evaluation of the learned target function.

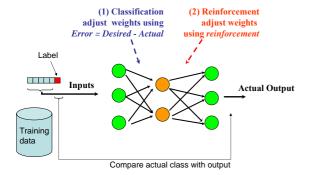
Criticism

- long training time.
- difficult to understand the learned function (weights).
- Typically for numerical data
- not easy to incorporate domain knowledge.
- Design can be tedious and error prone (Too small: slow learning - Too big: instability or poor performance)

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Learning Paradigms



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Learning Algorithms

· Back propagation for classification

- · Kohonen feature maps for clustering
- Recurrent back propagation for classification
- · Radial basis function for classification
- Adaptive resonance theory
- · Probabilistic neural networks

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Major Steps for Back Propagation Network

- · Constructing a network
 - input data representation
 - selection of number of layers, number of nodes in each layer.
- Training the network using training data
- · Pruning the network
- · Interpret the results

Network Training

- The ultimate objective of training
 - obtain a set of weights that makes almost all the tuples in the training data classified correctly.
- Steps:
 - Initial weights are set randomly.
 - Input tuples are fed into the network one by one.
 - Activation values for the hidden nodes are computed.
 - Output vector can be computed after the activation values of all hidden node are available.
 - Weights are adjusted using error (desired output actual output) and propagated backwards.

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Network Pruning

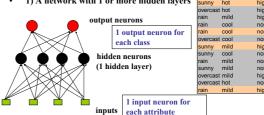
- Fully connected network will be hard to articulate
- *n* input nodes, *h* hidden nodes and *m* output nodes lead to h(m+n) links (weights)
- Pruning: Remove some of the links without affecting classification accuracy of the network.

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Backpropagation Network - Architecture

1) A network with 1 or more hidden layers



- 2) Feedforward network each neuron receives input only from the neurons in the previous laver
- 3) Typically fully connected all neurons in a layer are connected with all neurons in the next laver
- 4) Weights initialization small random values, e.g. [-1,1]

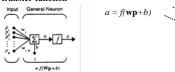
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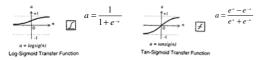
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Backpropagation Network – Architecture 2

5) Neuron model - weighed sum of input signals + differentiable transfer function



• any differentiable transfer function f can be used; most frequently the sigmoid and tan-sigmoid (hyperbolic tangent sigmoid) functions are used:

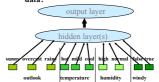


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Architecture – Number of Input Units

- Numerical data typically 1 input unit for each attribute
- Categorical data 1 input unit for each attribute value)
 - How many input units for the weather data?



Outlook	Tempreature	Humidity	Windy	Play
sunny	hot	high	false	No
sunny	hot	high	true	No
overcast	hot	high	false	Yes
rain	mild	high	false	Yes
rain	cool	normal	false	Yes
rain	cool	normal	true	No
overcast	cool	normal	true	Yes
sunny	mild	high	false	No
sunny	cool	normal	false	Yes
rain	mild	normal	false	Yes
sunny	mild	normal	true	Yes
overcast	mild	high	true	Yes
overcast	hot	normal	false	Yes
rain	mild	high	true	No

Encoding of the input examples – typically binary depending on the value of the

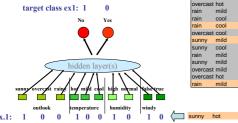
attribute (on and off) e.g.: 100 100 10 01

Other possibilities are also acceptable. For example "Windy" could be coded with only one unit: true or false (1 or 0).

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Number of Output Units





Outlook	Tempreature	Humidity	Windy	Play
sunny	hot	high	false	No
sunny	hot	high	true	No
overcast	hot	high	false	Yes
rain	mild	high	false	Yes
rain	cool	normal	false	Yes
rain	cool	normal	true	No
overcast	cool	normal	true	Yes
sunny	mild	high	false	No
sunny	cool	normal	false	Yes
rain	mild	normal	false	Yes
sunny	mild	normal	true	Yes
overcast	mild	high	true	Yes
overcast	hot	normal	false	Yes
rain	mild	high	true	No

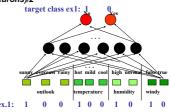
Encoding of the targets (classes) - typically binary e.g. class1 (no): 1 0, class2 (ves): 0 1

> Another possibility is to code the target class with only one unit: Yes or No (1 or 0).

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Number of Hidden Layers and Units in Them

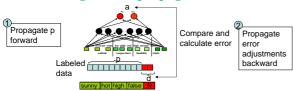
- An art! Typically by trial and error
- The task constrains the number of inputs and output units but not the number of hidden layers and neurons in them
 - Too many hidden layers and units (i.e. too many weights) overfitting
 - Too few underfitting, i.e. the NN is not able to learn the input-output mapping
 - A heuristic to start with: 1 hidden layer with n hidden neurons, n=(inputs+output_neurons)/2



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Learning in Backpropagation NNs



Idea of backpropagation learning

For each training example p

- Propagate p through the network and calculate the output a. Compare the desired d with the actual output a and calculate the error;
- Update weights of the network to reduce the error;

Until error over all examples < threshold

Why "backpropagation"? Adjusts the weights backwards (from the output to the input units) by propagating the weight change Δw

$$w_{pq}^{new} = w_{pq}^{old} + \Delta w_{pq}$$
 How to calculate the weight change?

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Backpropagation Learning - 2

- Sum of Squared Errors (E) is a classical measure of error
 - E for a single training example over all output neurons
 - d_i:desired, a_i:actual network output for output neuron i

$$E = \frac{1}{2} \sum_{i} e_{i}^{2} = \frac{1}{2} \sum_{i} (d_{i} - a_{i})^{2}$$

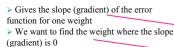
- Thus, backpropagation learning can be viewed as an optimization search in the weight space
 - Goal state the set of weights for which the performance index (error) is minimum
 - Search method hill climbing [reduce error for each training example]

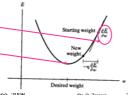
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Steepest Gradient Descent

- The direction of the steepest descent is called gradient and can be computed (\delta E/\delta w)
- A function decreases most rapidly when the direction of movement is in the direction of the negative of the gradient
- Hence, we want to adjust the weights so that the change moves the system down the error surface in the direction of the locally steepest descent, given by the negative of the gradient
- η learning rate, defines the step; typically in the range (0,1)

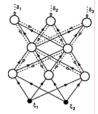




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Backpropagation Algorithm - Idea

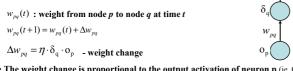
- The backpropagation algorithm adjust weights by working backward from the output layer to the input layer
- Calculate the error and propagate this error from layer to layer
- 2 approaches
 - Incremental the weights are adjusted after each training example is applied
 - · Called also an approximate steepest descent
 - · Preferred as it requires less space
 - Batch weights are adjusted once after all training examples are applied and a total error was calculated



- Solid lines forward propagation of signals
- Dashed lines backward propagation of error

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Backpropagation Rule - Delta change



- The weight change is proportional to the output activation of neuron p (ie. O_p) and the error δ of neuron q (ie. δ_p)
- δ is calculated in 2 different ways
 - q is an output neuron $\delta_q = (d_q o_q) \cdot (f'(net_q))$ • q is a hidden neuron $\delta_q = f'(net_q) \sum w_{qi} \delta_i$ (*i* is over the nodes

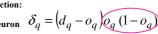
Derivative of the activation function at neuron q with respect to the input of q (netq)

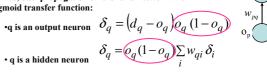
Derivative of Sigmoid Activation Function

• From the formulas for δ , we must be able to calculate the derivatives for f. For a sigmoid transfer function: $f(net_m) = o_m = \frac{1}{1 + e^{-net_m}}$

$$f'(net_m) = \frac{\partial o_m}{\partial net_m} = \frac{\partial \left(\frac{1}{1 + e^{-net_m}}\right)}{\partial net_m} = \frac{e^{-net_m}}{e^{-net_m}} = \frac{e^{-net_m$$

· Thus, backpropagation errors for a network with sigmoid transfer function:





$$\delta_q = o_q (1 - o_q) \sum_i w_{qi} \, \delta$$

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Backpropagation Algorithm - Summary

- 1. Determine the architecture of the network
 - how many input and output neurons; what output encoding
 - · hidden neurons and layers
- 2. Initialize all weights (biases incl.) to small random values, typically $\in [-1,1]$
- 3. Repeat until termination criterion satisfied:
 - •(forward pass) Present a training example and propagate it through the network to calculate the actual output
 - ullet (backward pass) Compute the error (the δ values for the output neurons). Starting with output layer, repeat for each layer in the network: - propagate the δ values back to the previous layer
 - update the weights between the two layers

- •The stopping criteria is checked at the end of each epoch: training s
 - · The error (mean absolute or mean square) is below a threshold
 - All training examples are propagated and the total error is calculated
 - · The threshold is determined heuristically e.g. 0.3
 - Maximum number of epochs is reached
 - · Early stopping using a validation set
- It typically takes hundreds or thousands of epochs for an NN to converge

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Some Interesting NN Applications

- · There are many examples of applications using
 - You can use them for the paper presentation in w12 and 13!
- Network design is typically the result of several months trial and error experimentation
- Moral: NNs are widely applicable but they cannot magically solve problems; wrong choices lead to poor performance
- "NNs are the second best way of doing just about anything" John Denker
 - NN provide passable performance on many tasks that would be difficult to solve explicitly with other techniques

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Lecture Outline

Part I: Artificial Neural Networks (ANN) (1 hour)

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 - What is an artificial neural network?
 - · Neuron model and activation function
 - Construction of a neural network
- Learning: Backpropagation Algorithm
 - Forward propagation of signal
 - · Backward propagation of error Example

Part II: Bayesian Classifiers (Statistical-based) (1 hour)

- What is Bayesian Classification
- Bayes theorem
- Naïve Bayes Algorithm
 - Using Laplace Estimate
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What is Bayesian Learning (Classification)?

- · Baysian classifiers are statistical classifiers
- They can predict the class membership probability, i.e. the probability that a given example belongs to a particular class.
- They are based on the Bayes Theorem, presented in the Essay Towards Solving a Problem in the Doctrine of Chances published posthumously by his friend Richard Price in the Philosophical Transactions of the Royal Society of London in

Thomas Bayes [1702-1761]

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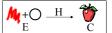
More on Bayesian Classifiers

- · It uses probabilistic learning by calculating explicit probabilities for hypothesis.
- A naïve Bayesian classifier, that assumes total independence between attributes, is commonly used for data classification and learning problems. It performs well with large data sets and exhibits high accuracy.
- The model is incremental in the sense that each training example can incrementally increase or decrease the probability that a hypothesis is correct. Prior knowledge can be combined with observed data

Bayes Theorem

- Given a data sample E (also called Evidence) with an unknown class label, H is the hypothesis that E belongs to a specific class C.
- The probability of a hypothesis H, P(H|E), probability of E conditioned on H, also called Posteriori Probability, follows the Bayes theorem:
- · Example: Instances of fruits, described by their colour and shape. Let E is red and round, *H* is the hypothesis that *E* is an

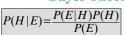
 $P(H|E) = \frac{P(E|H)P(H)}{P(H)}$

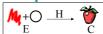


P(H)=P(♥)
 P(E) = P(♠+○)
 P(E|H)=P(♠+○if ♥)

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Bayes Theorem The Fruit Example





- P(H|E) reflects our confidence that E is an apple given that we have seen that E is red and round
 P(H|E)=P(*) if (*, O)
 - Called posterior, or posteriori probability, of H conditioned on E
- - Called prior, or apriori probability, of H
- The posteriori probability is based on more information that the apriori probability which is independent of E
- What is P(E/H)?

- the posterior probability of *E* conditioned on *H*: the probability that
 E is red and round given that we know that *E* is an apple.
- What is P(E)
- P(E)=P(/4 ,O)
- the prior probability of E: the probability that an example from the fruit data set is red and round

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Bayes Theorem - How to use it for classification?

$$P(H|E) = \frac{P(E|H)P(H)}{P(E)}$$

- In classification tasks we would like to predict the class of a new example E. We can do this by:
 - Calculating P(H|E) for each H (class) the probability that the hypothesis H is true given the example E
 - Comparing these probabilities and assigning E to the class with the highest probability.
 - How to estimate P(E), P(H) and P(E|H)?
 - From the given data (this is the training phase of the classifier)

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Naïve Bayes Classifier

Suppose we have n classes C₁, C₂,...,C_n. Given an unknown sample X, the classifier will predict that X=(x₁,x₂,...,x_n) belongs to the class with the highest posteriori probability:

 $X \in C_i$ if $P(C_i|X) > P(C_j|X)$ for $1 \le j \le n$, $j \ne i$

Maximize $\frac{P(X|C_i)P(C_i)}{P(X)}$

→ maximize P(X|C_i)P(C_i)

- $P(C_i) = s_i/s$
- $P(X|C_i) = \prod_{k=1}^{n} P(x_k | C_i)$ where $P(x_k | C_i) = s_{ik}/s_i$
- Greatly reduces the computation cost, only count the class distribution.
- Naïve: class conditional independence

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Naïve Bayes Algorithm - Basic Assumption

- Naïve Bayes uses all attributes to make a decision and allows them to make contributions to the decision that are equally important & independent of one another
 - Independence assumption attributes are conditionally independent of each other given the class
 - Equally importance assumption attributes are equally important
 - Unrealistic assumptions! => it is called *Naïve* Bayes
 - Are dependent of one another
 - Attributes are not equally important

We need to calculate P(yes|E) and P(no|E)

If we denote the 4 pieces of evidence

 But these assumptions lead to a simple method which works surprisingly well in practice!

Naïve Bayes for the Tennis Example - 2

where E is Outlook Tempreature Humidity Windy Play sunny cool high true ??

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Naïve Bayes (NB) for the Tennis Example

- Consider the tennis data
- Suppose we encounter a new example which has to be classified:

 Outlook
 Tempreature Humidity Windy
 Play

 sunny
 cool
 high
 true
 ??

Recall the Bayes theorem:

$$P(H \mid E) = \frac{P(E \mid H)P(H)}{P(E)}$$

sunny hot high false No sunny hot high true No overcast hot high false Yes rain cool normal false Yes rain cool normal false Yes sunny mild high false No sunny cool normal false Yes sunny mild high false No sunny mild normal false Yes rain mild normal false Yes overcast mild high true Yes overcast mild high true Yes overcast hot normal false Yes



What are H & E for our example?

- the hypothesis H is that the class is P (and there is another hypothesis: that the class is N)
- the evidence E is the new example (i.e. a particular combination of observed attribute values for the new day)

humidity=high with E₃
 windy=true with E₄

outlook=sunny with with E₁

- temperature=cool with E2

 $P(H \mid E) = \frac{P(E \mid H)P(H)}{P(H)}$

and <u>assume that they are independent given the class</u>, than their combined probability is obtained by multiplication:

 $P(E \mid yes) = P(E_1 \mid yes) P(E_2 \mid yes) P(E_3 \mid yes) P(E_4 \mid yes)$

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Naïve Bayes for the Tennis Example - 3

Hence

$$P(yes \mid E) = \frac{P(E_1 \mid yes)P(E_2 \mid yes)P(E_3 \mid yes)P(E_4 \mid yes)P(yes)}{P(E)}$$

- Probabilities in the numerator will be estimated from the data.
- There is no need to estimate P(E) as it will appear also in the denominators of the other hypotheses, i.e. it will disappear when we compare them.

$$P(no \mid E) = \frac{P(E_1 \mid no) P(E_2 \mid no) P(E_3 \mid no) P(E_4 \mid no) P(no)}{P(E)}$$

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Naïve Bayes for the Tennis Example -

Tennis data - counts and probabilities:

Outlook	Tempreature	Humidity	Windy	Play
sunny	hot	high	false	No
sunny	hot	high	true	No
overcast	hot	high	false	Yes
rain	mild	high	false	Yes
rain	cool	normal	false	Yes
rain	cool	normal	true	No
overcast	cool	normal	true	Yes
sunny	mild	high	false	No
sunny	cool	normal	false	Yes
rain	mild	normal	false	Yes
sunny	mild	normal	true	Yes
overcast	mild	high	true	Yes
overcast	hot	normal	false	Yes
rain	mild	high	true	No

proportions of days when play is ves

proportions of days when humidity is normal and play is yes i.e. the probability of humidity to be normal given that play is yes

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Naïve Bayes for the Tennis Example - cont.2

 $P(yes \mid E) = \frac{P(E_1 \mid yes) P(E_2 \mid yes) P(E_3 \mid yes) P(E_4 \mid yes) P(yes)}{P(yes \mid E)}$ $P(yes \mid E) = ?$ P(E)2/5 (9/14) 5/14

- ⇒ P(E₁|yes)=P(outlook=sunny|yes)=2/9 P(E2|yes)=P(temperature=cool|yes)=3/9 P(E₃|yes)=P(humidity=high|yes)=3/9 P(E4|yes)=P(windy=true|yes)=3/9
- P(yes) =? the probability of a Play=yes without knowing any E, i.e. anything about the particular day; the prior probability of yes; P(Play=yes) = 9/14 33459-01: Principles of Knowledge Discovery in Data – March-June, 2006

Naïve Bayes for the Tennis Example - cont.3

. By substituting the respective evidence probabilities:

$$P(yes \mid E) = \frac{\frac{2}{9} \frac{3}{9} \frac{3}{9} \frac{9}{9} \frac{9}{14}}{P(E)} = \frac{0.0053}{P(E)}$$

• Similarly calculating: $P(no \mid E)$

	31435	
$P(no \mid E) =$	555514	-0.0206
I(no L) =	P(E)	P(E)

- $\Rightarrow P(no|E) > P(yes|E)$
- => for the new day play = no is more likely than play = yes (4 times more likely)

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A Problem with Naïve Bayes

- Suppose that the training data for the tennis example was different:
 - outlook=sunny had been always associated with play=no (i.e. outlook=sunny had never occurred together with play=yes $)\,$
- - P(yes|outlook=sunny)=0 and P(no|outlook=sunny)=1

$$P(yes \mid E) = \underbrace{P(E_1 \mid yes)P(E_2 \mid yes)P(E_3 \mid yes)P(E_4 \mid yes)P(yes)}_{=\mathbf{0}}$$

- => final probability P(yes|E)=0 no matter of the other probabilities, i.e. zero probabilities hold a veto over the other probabilities
- This is a problem!
 - If it happens in the training set => poor prediction on new data
- Solution: use Laplace estimator (correction) to calculate probabilities
 - Adds 1 to the numerator and k to the denominator, where k is the number of attribute values for a given attribute

Laplace Correction – Modified Tennis Example

	outlook		
	yes	no	:
sunny	0	5	
overcast	4	0	:
rainy	3	2	:
sunny	0/7	5/7	
overcast	4/7	0/7	:
rainy	3/7	2/7	

P(sunny|yes)=0/7 P(overcast|yes)=4/7 P(rainy|yes)=3/7

· Laplace correction adds 1 to the numerator and 3 to the denominator

$$P(sunny | yes) = \frac{0+1}{7+3} = \frac{1}{10} = 0.1$$

 $P(overcast | yes) = \frac{4+1}{7+3} = \frac{5}{10} = 0.5$

 $P(overcast \mid yes) = \frac{4+1}{7+3} = \frac{5}{10} = 0.5$

$$P(rainy \mid yes) = \frac{3+1}{7+3} = \frac{4}{10} = 0.4$$

Ensures that an attribute value which occurs 0 times will receive a nonzero (although small) probability.

Laplace Correction – Original Tennis Example

	outlook		
	yes	no	:
sunny	2	3	
overcast	4	0	:
rainy	3	2	
	(:
sunny	(2/9)	3/5	
overcast	4/9	0/5	:
rainv	(3/9)	2/5	

P(sunny|yes)=2/9 P(overcast|yes)=4/9 P(rainy|yes)=3/9

$$P(sunny \mid yes) = \frac{2+1}{9+3} = \frac{3}{12} = 0.25$$

$$P(overcast \mid yes) = \frac{4+1}{9+3} = \frac{5}{12} = 0.416$$

$$P(rainy \mid yes) = \frac{3+1}{9+3} = \frac{4}{12} = 0.33$$

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Handling Missing Values

- · Easy:
 - Missing value in the evidence E (the new example) omit this attribute

e.g. E: outlook=?, temperature=cool, humidity=high, windy=true

Problem
$$P(yes \mid E) = \frac{\frac{3}{9} \frac{3}{9} \frac{3}{9} \frac{9}{14}}{P(E)} = \frac{0.0238}{P(E)} P(no \mid E) = \frac{\frac{1}{5} \frac{4}{5} \frac{3}{5} \frac{5}{14}}{P(E)} = \frac{0.0343}{P(E)}$$

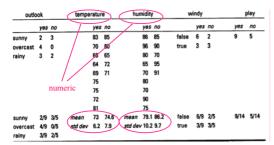


- · Compare these results with the previous!
- as one of the fractions is missing, the probabilities are higher then before, but this is not a problem as there is a a missing fraction in
- Missing value in the training example:
 - do not include them in the frequency counts and calculate the probabilities based on the number of values that actually occur and not on the total number of training examples

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Handling Numeric Attributes



• We would like to classify the following new example: outlook=sunny, temperature=66, humidity=90, windv=true



· Q. How to calculate P(temperature=66|yes), P(humidity=90|yes), P(temperature=66|no), P(humidity=90|no)?

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Using Probability Density Function

- · A. By assuming that numerical values have a normal (Gaussian) probability distribution and using probability density function
- For a *normal* distribution with mean μ and standard deviation o, the probability density function is:



$$f(x) = \frac{1}{\sigma\sqrt{2\pi}}e^{\frac{-(x-\mu)^2}{2\sigma^2}}$$

- · What is the meaning of the probability density function of a continuous random variable?
 - Closely related to probability but is not exactly the probability (e.g. the probability that x is exactly 66 is 0)
- The probability that a given value x takes a value in a small region (between x- ϵ /2 and x + ϵ /2) is ϵ f(x) (e.g. that probability that x is between 64 and 68 is f(x)) 33459-01: Principles of Knowledge Discovery in Data – March-June, 2006 (Dr. O. Zalane)

Calculating Probabilities Using Probability **Density Function**

$$f(temperature = 66 \mid yes) = \frac{1}{6.2\sqrt{2\pi}}e^{\frac{-(66-73)^2}{2^*6.2^2}} = 0.034$$

f(humidity = 90 | yes) = 0.0221

$$P(yes \mid E) = \frac{\frac{2}{9} \cdot 0.034 \cdot 0.0221 \frac{3}{9} \frac{9}{14}}{P(E)} = \frac{0.000036}{P(E)} = > P(no \mid E) > P(yes \mid E)$$

$$= P(no \mid E) = \frac{\frac{3}{5} \cdot 0.0291 \cdot 0.038 \frac{3}{5} \frac{5}{14}}{P(E)} = \frac{0.000136}{P(E)}$$



Compare with the categorical tennis data!

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=>P(no|E)>P(yes|E)

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Naïve Bayes - Advantages & Disadvantages

- · Advantages:
 - simple approach
 - clear semantics for representing, using and learning probabilistic knowledge
 - requires 1 scan of the training data
 - in many cases outperforms more sophisticated learning methods → always try the simple method first!
- · Disadvantages:
 - While there is only 1 scan, it is still computationally expensive
 - since attributes are treated as though they were completely independent, the existence of dependencies between attributes skews the learning process!
 - Normal distribution assumption when dealing with numeric attributes - (minor) restriction → discretize the data or follow other distributions

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Belief Network

- Allows class conditional dependencies to be expressed.
- It has a directed acyclic graph (DAG) and a set of conditional probability tables (CPT).
- Nodes in the graph represent variables and arcs represent probabilistic dependencies. (child dependent on parent)
- There is one table for each variable X. The table contains the conditional distribution P(X|Parents(X)).

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LungCancer (Emphysema)

Smoker

Dyspnea

Family

History

PositiveXRa

(FH, S) (FH, ~S)(~FH, S) (~FH, ~S)

LC 0.8 0.5 0.7 0.1

The conditional probability table for the variable LungCancer

0.2

Bayesian Belief Networks

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0.3

0.9

Bayesian Belief Networks

Several cases of learning Bayesian belief networks:

- When both network structure and all the variables are given then the learning is simply computing the CPT.
- When network structure is given but some variables are not known or observable, then iterative learning is necessary (compute gradient InP(S|H), take steps toward gradient and normalize).
- Many algorithms for learning the network structure exist

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Classification Methods

Bayesian Belief Networks

Example

~LC



- Support Vector Machines
- ❖ Case-Based Reasoning
- Genetic Algorithms
- * Rough Set Theory
- Fuzzy Sets
- **&** Etc.

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Lecture Outline

Part III: k-Nearest Neighbour (30 minutes

- Lazy Learning
 - Nearest Neighbour
 - K-Nearest neighbours
- Agglomerative Nearest Neighbours

Part IV: Decision Trees (1 hour)

- What is a Decision Tree?
- Building a tree
- Pruning a tree

Part V: Associative Classifiers (1 hour)

- Rule Generation
- Rule Pruning
- Rule Selection
- Rule Combination

k-Nearest Neighbours (k-NN)
Classification

- In k-nearest-neighbour classification, the training dataset is used to classify each member of a "target" dataset.
- There is no model created during a learning phase but the training set itself.
- It is called a *lazy-learning* method.
- Rather than building a model and referring to it during the classification. K-NN directly refers to the training set for classification.

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The Simple Nearest Neighbour Approach

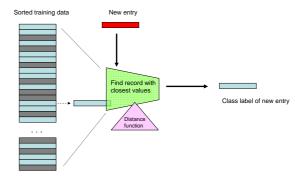
- Nearest Neighbour is very simple. The training is nothing more than sorting the training data and storing it in a list.
- To classify a new entry, this entry is compared to the list to find the closest record, with value as similar as possible to the entry to classify (i.e. nearest neighbour). The class of this record is simply assigned to the new entry.
- Different measures of similarity or distance can be used.

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The Nearest Neighbour



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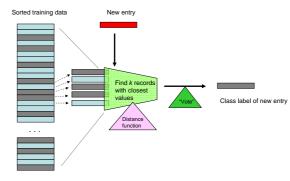
The k-Nearest Neighbour Approach

- The k-Nearest Neighbour is a variation of Nearest Neighbour. Instead of looking for only the closest record to the entry to classify, we look for the k records closest to it.
- To assign a class label to the new entry, from all the labels of the k nearest records we take the majority class label.
- Nearest Neighbour is a case of k-Nearest Neighbours with k=1.

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k Nearest Neighbours



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Agglomerative Nearest Neighbours

- Training records are put together in groups as the learning process goes on. The approach is named agglomerative because groups or clusters are merged during the learning.
- · The training is relatively simple:
 - Each cluster has a center c and a radius r and the class label of its records. Initially each record in the training set forms a cluster on its own.
 - Two clusters that are close together (within some epsilon distance of each other) and classify the same category are combined to build a new aggregate cluster: a hypersphere of a larger radius and a new center.
 - If a cluster is not close to any other clusters given epsilon, it remains separate.

Agglomerative NN Classification

- The classification of a new entry consists of finding the closest cluster to it and assign it the label attached to that cluster.
- Agglomerative NN has a slower training than NN or k-NN but has the advantage of using less memory. There is no need to store all the training set but only the center and radius of each cluster.
- In the two extremes: if all records are far from each other they remain separate clusters → Nearest Neighbour. If all points are close to each other we end-up with as many clusters as we have classes.

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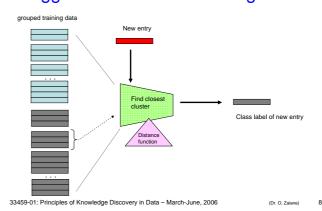
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Cluster Overlap Problem

- · Since clusters are hyperspheres, overlap of clusters of different labels are bound to happen.
- Clusters that grow and overlap with nearby clusters that classify differently can reduce accuracy. A new entry that falls in an overlap area between two clusters can easily be misclassified.
- · One solution is to inhibit clusters from growing if enlarging a hypersphere would generate overlap with a different class label cluster, and simply create new a small cluster in between.



Agglomerative Nearest Neighbours



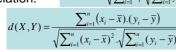
Distance Measures

- The most used distance function is the Euclidian distance: $d(X,Y) = \sqrt{\sum_{i=1}^{n} (x_i - y_i)^2}$
- However, other measures are possible
 - $d(X,Y) = \sum_{i=1}^{n} (x_i y_i)$ - the Manhattan distance:
 - $d(X,Y) = \max_{i=1}^{n} (x_i y_i)$ - the Chebychev:
 - the cosine measure:

- Pearson's correlation:







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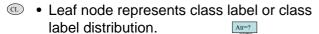
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What is a Decision Tree?

A decision tree is a flow-chart-like tree structure.

- Internal node denotes a test on an attribute
 - Branch represents an outcome of the test
 - All tuples in branch have the same value for the tested attribute.



Example from Quinlan's ID3

An

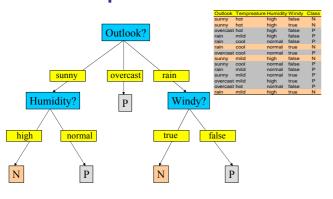
Outlook	Tempreature	Humidity	Windy	Class
sunny	hot	high	false	N
sunny	hot	high	true	N
overcast	hot	high	false	Р
rain	mild	high	false	Р
rain	cool	normal	false	Р
rain	cool	normal	true	N
overcast	cool	normal	true	Р
sunny	mild	high	false	N
sunny	cool	normal	false	Р
rain	mild	normal	false	Р
sunny	mild	normal	true	Р
overcast	mild	high	true	Р
overcast	hot	normal	false	Р
rain	mild	high	true	N

Training Dataset

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A Sample Decision Tree



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Decision-Tree Classification Methods

The basic top-down decision tree generation approach usually consists of two phases:

1. Tree construction

- At the start, all the training examples are at the root.
- Partition examples are recursively based on selected attributes.

2. Tree pruning

· Aiming at removing tree branches that may reflect noise in the training data and lead to errors when classifying test data → improve classification accuracy.

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Decision Tree Construction

Recursive process:

- Tree starts a single node representing all data.
- If sample are all same class then node becomes a leaf labeled with class label.
- Otherwise, select attribute that best separates sample into individual classes
- Recursion stops when:
 - Sample in node belong to the same class (majority);
 - There are no remaining attributes on which to split;
 - There are no samples with attribute value.

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Choosing the Attribute to Split Data Set

- The measure is also called Goodness function
- Different algorithms may use different goodness functions:
 - information gain (ID3/C4.5)
 - · assume all attributes to be categorical.
 - · can be modified for continuous-valued attributes.

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- assume all attributes are continuous-valued.
- · assume there exist several possible split values for each attribute.
- may need other tools, such as clustering, to get the possible split values.
- · can be modified for categorical attributes.

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Information Gain (ID3/C4.5)

- Assume that there are two classes, P and N.
 - Let the set of examples S contain x elements of class P and y elements of class N.
 - The amount of information, needed to decide if an arbitrary example in S belong to P or N is defined as:

$$I(S_{P}, S_{N}) = -\frac{x}{x+y} \log \frac{x}{x+y} - \frac{y}{x+y} \log \frac{y}{x+y}$$

- Assume that using attribute A as the root in the tree will partition S in sets $\{S_1, S_2, ..., S_v\}$.
 - If S_i contains x_i examples of P and y_i examples of N, the information needed to classify objects in all subtrees S_i :

$$E(A) = \sum_{i=1}^{\nu} \frac{x_i + y_i}{x + y} I(S_{P_i}, S_{N_i})$$

 $E(A) = \sum_{i=1}^{v} \frac{x_i + y_i}{x + y} I(S_{P_i}, S_{N_i}) \quad \text{In general} \quad E(A) = \sum_{i=1}^{v} \frac{S_{1i} + S_{2i} + \dots + S_{ni}}{s} I(s_{1i}, s_{2i}, \dots, s_{ni})$

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Information Gain -- Example

• The attribute A is selected such that the *information gain* $gain(A) = I(S_P, S_N) - E(A)$

is maximal, that is, E(A) is minimal since $I(S_P, S_N)$ is the same to all attributes at a node.

In the given sample data, attribute outlook is chosen to split at the root:

gain(outlook) = 0.246gain(temperature) = 0.029 gain(humidity) = 0.151

Information gain measure tends to favor attributes with many values. Other possibilities: Gini Index, χ^2 , etc.

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gain(windy) = 0.048

Gini Index

- If a data set S contains examples from n classes, gini index, gini(S) is defined as $gini(S) = 1 - \sum_{n=1}^{\infty} p^{2}$
 - where p_i is the relative frequency of class j in S.
- If a data set S is split into two subsets S_1 and S_2 with sizes N_1 and N_2 respectively, the *gini* index of the split data contains examples from n classes, the gini index gini(S) is defined as

 $gini_{split}(S) = \frac{N_1}{N}gini(S_1) + \frac{N_2}{N}gini(S_2)$

The attribute that provides the smallest $gini_{split}(S)$ is chosen to split the node (need to enumerate all possible splitting points for each attribute).

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Example for gini Index

- Suppose there two attributes: age and income, and the class label is buy and not buy.
- There are three possible split values for age: 30, 40.50.
- There are two possible split values for income: 30K, 40K
- We need to calculate the following gini index
 - gini age = 30 (S),
 - gini age = 40 (S),
 - gini age = 50 (S),
 - gini income = 30k (S),
 - gini income = 40k (S)
- Choose the minimal one as the split attribute

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Primary Issues in Tree Construction

- · Split criterion:
 - Used to select the attribute to be split at a tree node during the tree generation phase.
 - Different algorithms may use different goodness functions: information gain, gini index, etc.
- · Branching scheme:
 - Determining the tree branch to which a sample belongs.
 - binary splitting (gini index) versus many splitting (information
- Stopping decision: When to stop the further splitting of a node, e.g. impurity measure.
- Labeling rule: a node is labeled as the class to which most samples at the node belong.

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How to construct a tree?

- Algorithm
 - greedy algorithm
 - · make optimal choice at each step: select the best attribute for each tree node.
 - top-down recursive divide-and-conquer manner
 - · from root to leaf
 - · split node to several branches
 - for each branch, recursively run the algorithm

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Example for Algorithm (ID3)

- · All attributes are categorical
- Create a node N;
 - if samples are all of the same class C, then return N as a leaf node labeled with C
 - if attribute-list is empty then return N as a left node labeled with the
- · Select split-attribute with highest information gain
 - label N with the split-attribute
 - for each value A_i of split-attribute, grow a branch from Node N
 - let S_i be the branch in which all tuples have the value A_i for splitattribute
 - if S_i is empty then attach a leaf labeled with the most common class.
 - · Else recursively run the algorithm at Node Si
- Until all branches reach leaf nodes

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Directly

- test the attribute value of unknown sample against the tree.

How to use a tree?

- A path is traced from root to a leaf which holds the label.
- Indirectly
 - decision tree is converted to classification rules.
 - one rule is created for each path from the root to a leaf
 - IF-THEN rules are easier for humans to understand.

Avoid Over-fitting in Classification

- A tree generated may over-fit the training examples due to noise or too small a set of training data.
- · Two approaches to avoid over-fitting:
 - (Stop earlier): Stop growing the tree earlier.
 - (Post-prune): Allow over-fit and then post-prune the tree.
- Approaches to determine the correct final tree size:
 - Separate training and testing sets or use cross-validation.
 - Use all the data for training, but apply a statistical test (e.g., chisquare) to estimate whether expanding or pruning a node may improve over entire distribution.
 - Use Minimum Description Length (MDL) principle: halting growth of the tree when the encoding is minimized.
- · Rule post-pruning (C4.5): converting to rules before pruning.

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Continuous and Missing Values in Decision-Tree Induction

Dynamically define new discrete-valued attributes that partition the continuous attribute value into a discrete set of intervals.

 Temperature 40 48 60 72 80 90 play tennis No No Yes Yes Yes No

- Sort the examples according to the continuous attribute A, then identify adjacent examples that differ in their target classification, generate a set of candidate thresholds midway, and select the one with the maximum gain.
- · Extensible to split continuous attributes into multiple intervals.
- · Assign missing attribute values either
 - Assign the most common value of A(x).
 - Assign probability to each of the possible values of A.

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Alternative Measures for Selecting Attributes

- · Info gain naturally favours attributes with many values.
- One alternative measure: gain ratio (Quinlan'86) which is to penalize attribute with many values.

SplitInfo
$$(S, A) \equiv -\sum \frac{|S_i|}{|S|} \log_2 \frac{|S_i|}{|S|}$$

GainRatio $(S,A) = \frac{Gain(S,A)}{SplitInfo(S,A)}$

- Problem: denominator can be 0 or close which makes GainRatio very large.
- Distance-based measure (Lopez de Mantaras'91):
 - define a distance metric between partitions of the data.
 - choose the one closest to the perfect partition.
- There are many other measures. Mingers'91 provides an experimental analysis of effectiveness of several selection measures over a variety of problems.

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e) :

Tree Pruning

- A decision tree constructed using the training data may have too many branches/leaf nodes.
 - Caused by noise, over-fitting.
 - May result poor accuracy for unseen samples.
- Prune the tree: merge a subtree into a leaf node.
 - Using a set of data different from the training data.
 - At a tree node, if the accuracy without splitting is higher than the accuracy with splitting, replace the subtree with a leaf node, label it using the majority class.
- Issues:
 - Obtaining the testing data.
 - Criteria other than accuracy (e.g. minimum description length).

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Pruning Criterion

- Use a separate set of examples to evaluate the utility of post-pruning nodes from the tree.
 - CART uses cost-complexity pruning.
- Apply a statistical test to estimate whether expanding (or pruning) a particular node.
 - C4.5 uses pessimistic pruning.
- Minimum Description Length (no test sample needed).
 - SLIQ and SPRINT use MDL pruning.

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Pruning Criterion --- MDL

- Best binary decision tree is the one that can be encoded with the fewest number of bits
 - Selecting a scheme to encode a tree
 - Comparing various subtrees using the cost of encoding
 - The best model minimizes the cost
- · Encoding schema
 - One bit to specify whether a node is a leaf (0) or an internal node (1)
 - loga bits to specify the splitting attribute
 - Splitting the value for the attribute:
 - categorical --- log(v-1) bits

• numerical --- log 2^{v - 2}

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Lecture Outline

Part III: k-Nearest Neighbour (30 minutes)

- Lazy Learning
 - Nearest Neighbour
 - K-Nearest neighbours
- Agglomerative Nearest Neighbours

Part IV: Decision Trees (1 hour)

- What is a Decision Tree?
- Building a tree
- Pruning a tree

Part V: Associative Classifiers (1 hour)

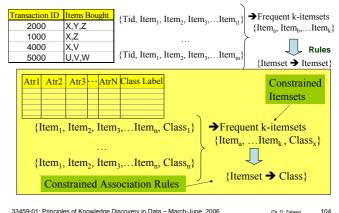
- Rule Generation
- Rule Pruning
- Rule Selection
- Rule Combination

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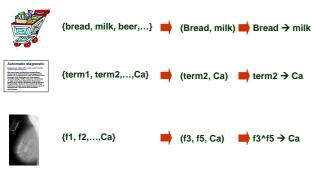
How do Associative Classifiers Work?



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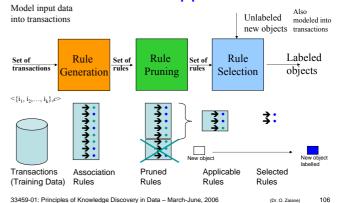
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Modeling documents

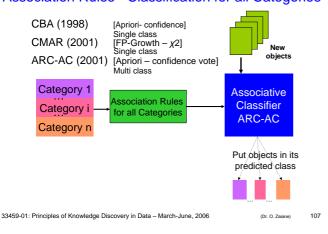


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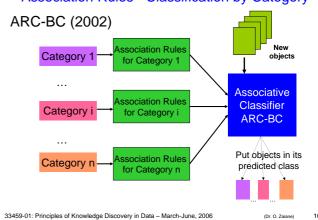
General Approach



Association Rules - Classification for all Categories



Association Rules - Classification by Category



Association Rules: Advantages & Issues

- AR are well studied fast
 - scalable
- · No independence assumption btw. attributes
- Attributes: large number
- variable number, can handle missing values
- Transparency
- · AC are in an early stage of development
 - use simple rules
 - naïve selection function
- AC models consist of a large number of rules
 - harder selection
 - redundant, uninteresting rules
 - longer classification time
 - difficult to manually revisit rules

Solution: Pruning Techniques

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Pruning Rules

Large number of rules

Noisy information

> Long classification time

Solution: Pruning Techniques

• Removing low ranked specialized rules;

$$R_1: F_1 \Rightarrow C$$
 Confidence 90%
 $R_2: F_1 \land F_2 \Rightarrow C$ Confidence 80% $=$

• Eliminate conflicting rules (for single-class classification);

$$F_1 \Rightarrow C_1 \land F_1 \Rightarrow C_2$$

· Database coverage;

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Classification Stage

Let S be the classification system

A new object O <f1; f3; f4; f7; f9 >

f1 → C1 confidence 0.9

f3 & f4 → C2 confidence 0.85

f4 → C2 confidence 0.8

f7 → C1 confidence 0.6 f9 → C3 confidence 0.5

C2 0.825 **C1** 0.75 **C3** 0.5

Using the *dominance factor* we chose the winning categories. If δ =100% C2 is winning. If δ =80% O is predicted to fall in C2 and C1.

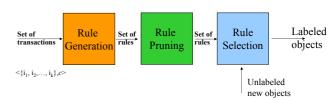
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Summary

Model input data into transactions



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Open Problems?

