

Modern Heuristic Search: Towards a Unifying Framework

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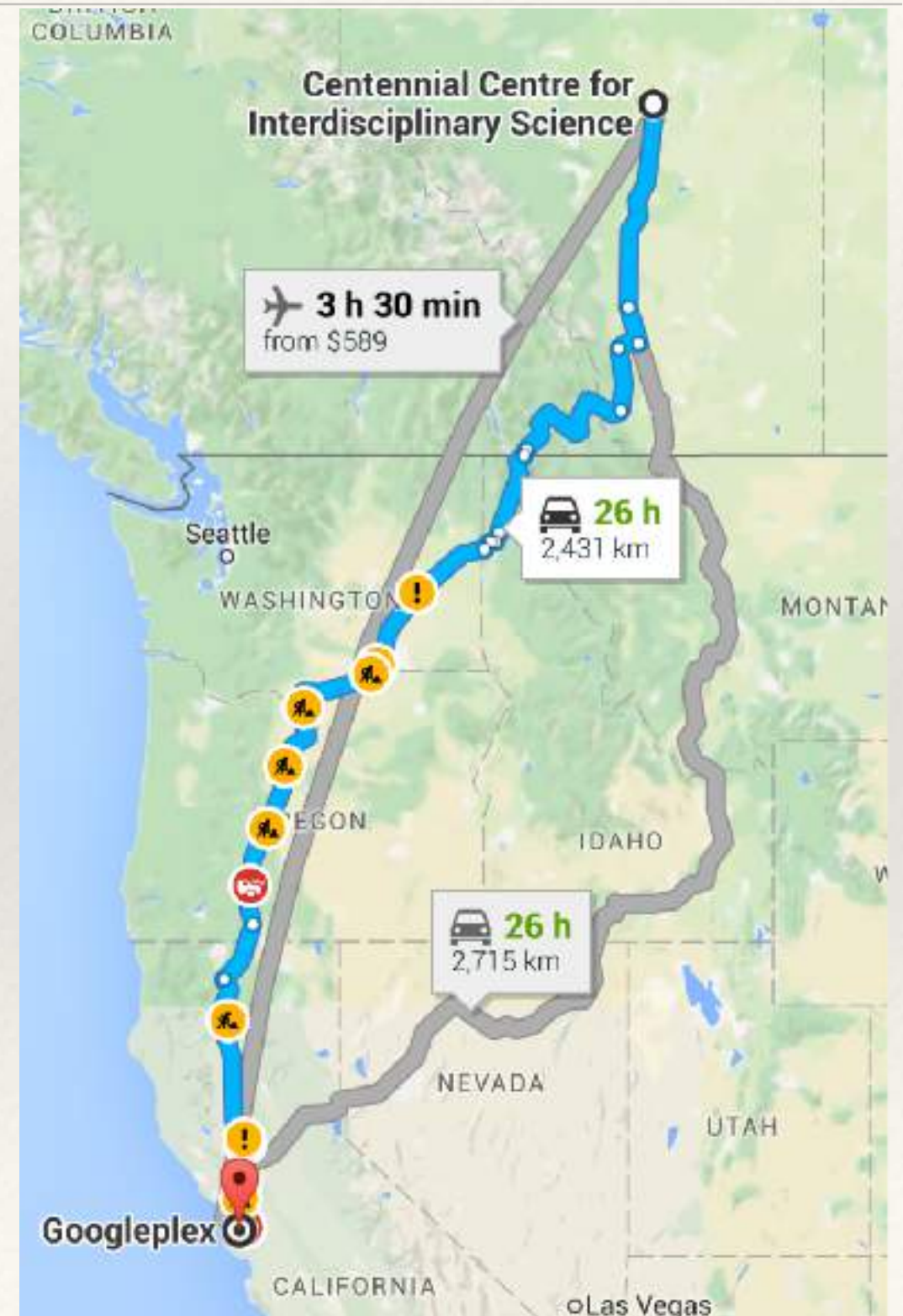
Outline of the Talk

- ❖ What is heuristic search?
- ❖ Some textbook examples
- ❖ What is different in modern heuristic search?
- ❖ Examples of recent work
- ❖ Towards a general framework

What is Heuristic Search?

Heuristic Search Example

- ❖ Heuristic search is a research area in computing science
- ❖ It is considered a part of the field of Artificial Intelligence
- ❖ It can be used for *sequential decision-making problems*
- ❖ Many applications: automated **planning**, optimization problems, pathfinding, **games**, puzzles,...

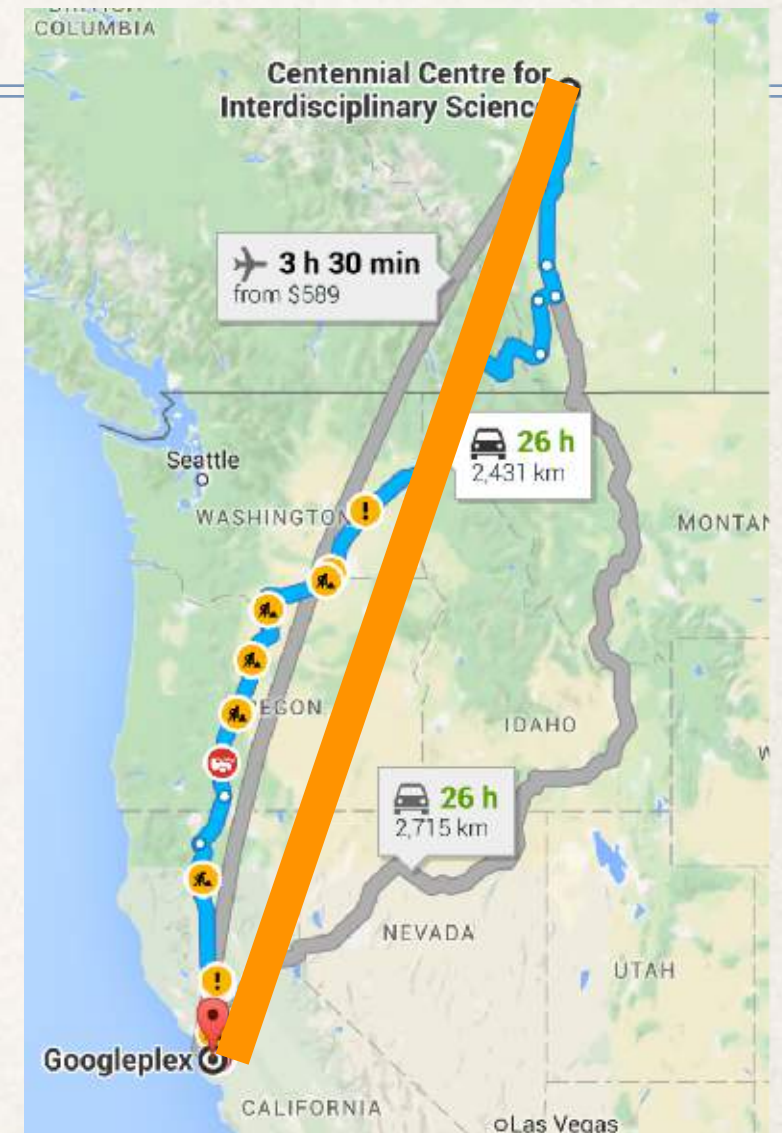


Which Kind of Search?

- ❖ There are many other kinds of search in computing science
 - ❖ Internet search, database search, binary search, ...
- ❖ In *heuristic search*, we search ahead into the future
 - ❖ Which sequences of actions can happen?
 - ❖ What is their effect?
 - ❖ Goal: make decisions about best actions

What is a Heuristic?

- ❖ Heuristic is a rough, inexact rule
- ❖ A heuristic can *guide* the search
 - ❖ Roughly, how good is an action?
 - ❖ Roughly, how good is a state?
- ❖ Main question: How to use them to make good decisions?



Heuristic:
straight-line distance

Why Use a Heuristic?

- ❖ Contrast: heuristic vs exact knowledge
- ❖ Why not use exact knowledge instead?
 - ❖ Often, it is simply not available
 - ❖ Example: how good is this Go position?
 - ❖ Sometimes, it is available but too expensive to compute
- ❖ Problem: how to build a **robust** system on inexact heuristics



Making Complex Decisions

- ❖ We make decisions every moment of our lives
- ❖ What is the process that leads to our decisions?
- ❖ How to make good decisions?
- ❖ Consider many alternatives
- ❖ Consider short-term and long-term consequences
- ❖ Evaluate different options and choose the best-looking one

Making Sequential Decisions

- ❖ Make decision:
 - ❖ Get current state of world
 - ❖ Analyze it
 - ❖ Select an action
 - ❖ Observe the world's response
 - ❖ If not done:
 - make another decision

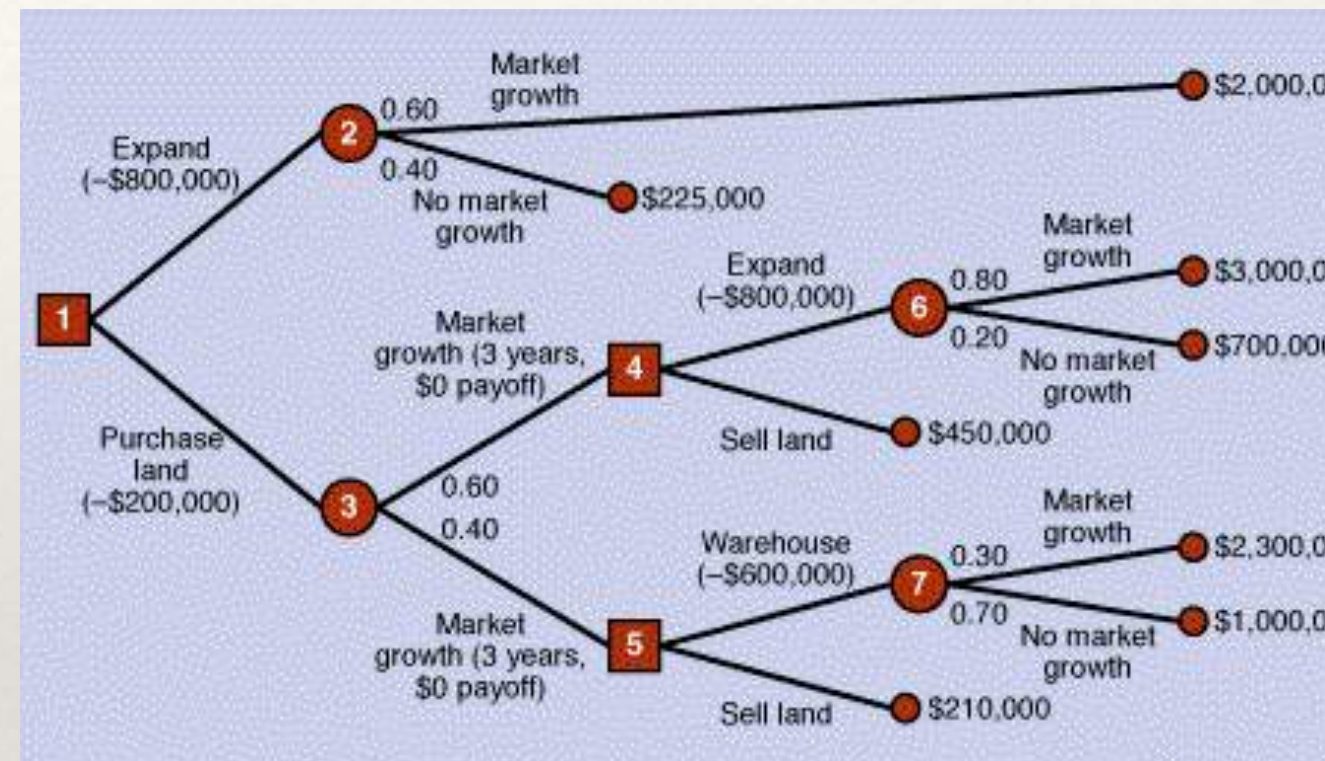
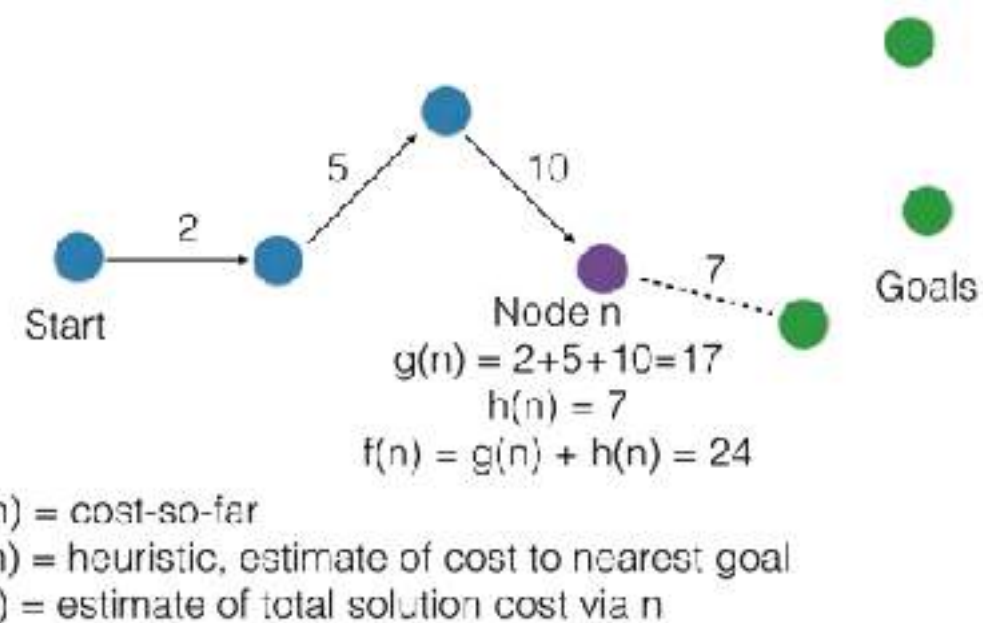


Image Source:
<http://www.prenhall.com>

Some Textbook Examples of Heuristic Search

A* Algorithm, Shortest Path

- ❖ State space with start state, end state
- ❖ Heuristic $h(s)$ estimates cost-to-go from s to goal
- ❖ $g(s)$ is cost-so-far from start to s
- ❖ A* always expands a node of smallest sum $g(s) + h(s)$
- ❖ Greedy, always follows heuristic, no other steps



Minimax, Alphabeta Algorithm

- ❖ Standard algorithm for game tree search
- ❖ Very successful for chess, checkers, many other games
- ❖ Tree search, then call heuristic evaluation function in leaf node
- ❖ Problem: always trusts the evaluation function, not robust against errors
- ❖ Mostly useless in Go, evaluation quality too bad

Main Problem of Classical Heuristic Search

- ❖ Classical methods have two main ingredients
 - ❖ Search algorithm
 - ❖ Knowledge expressed as heuristic (evaluation) function
- ❖ Problem: search is greedy / naive
 - ❖ Always trusts the heuristic
 - ❖ Not robust against errors in heuristic
 - ❖ Search can amplify the errors

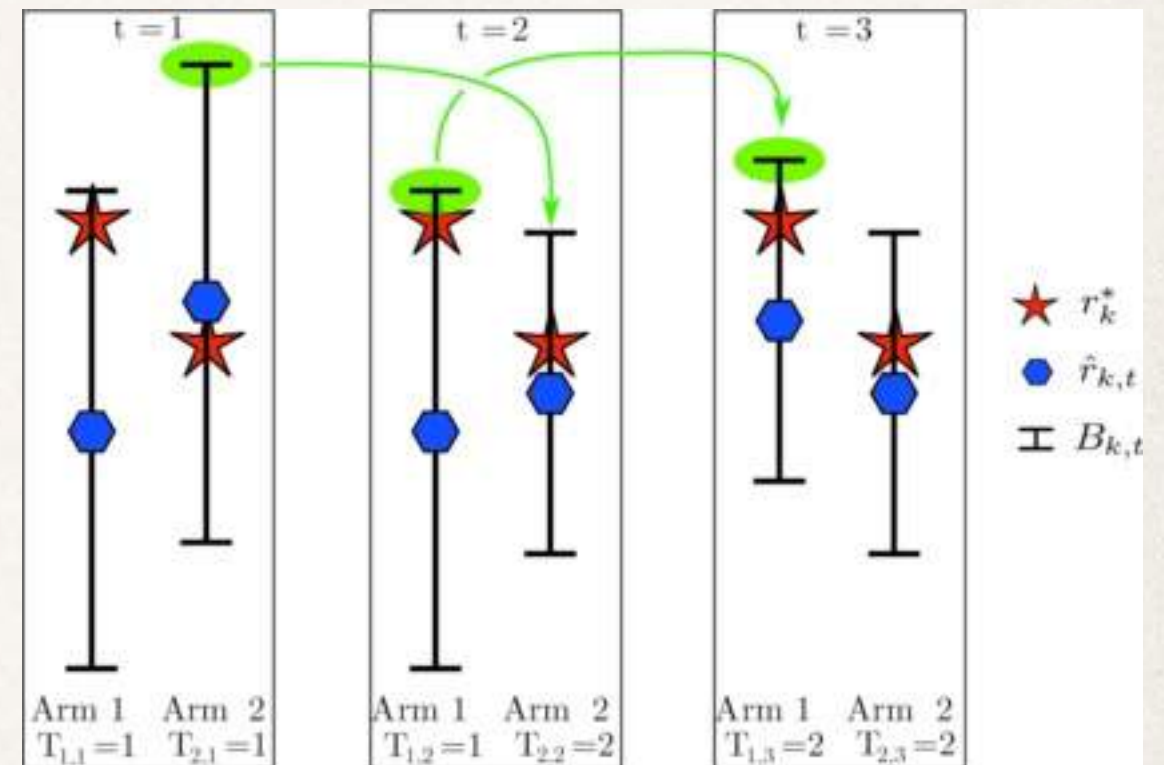
What is Different in Modern Heuristic Search?

Exploration and Exploitation

- ❖ We often deal with information that is:
 - ❖ Heuristic, incomplete, stochastic, sparse,...
- ❖ Fundamental trade-off:
 - ❖ **Exploitation:** make decision based on the information we have
 - ❖ **Exploration:** go find more information

Exploration Algorithm for Bandit Problems

- ❖ Different actions, unknown “payoff” value
- ❖ Can sample each action, at a cost
- ❖ Value of action = expected payoff
- ❖ Uncertainty about value from lack of samples



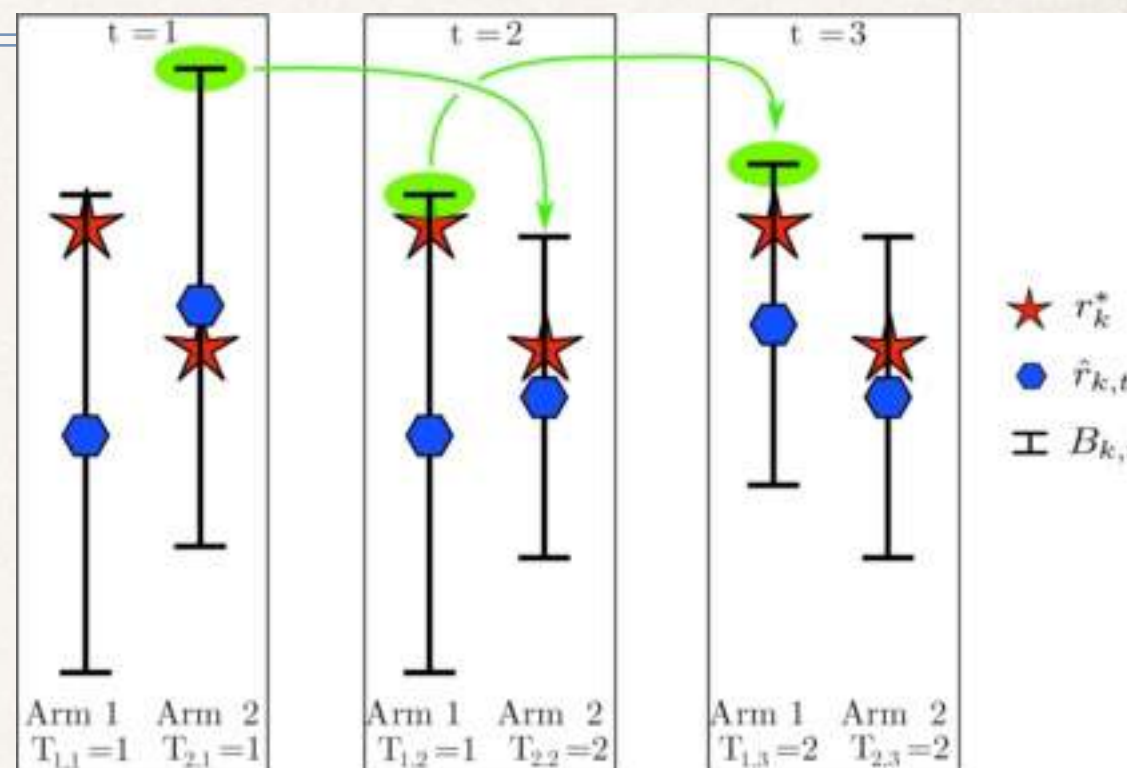
Bandit Problems and UCB

- ❖ Explore = get more statistics

- ❖ Exploit = play best action

- ❖ UCB combines both ideas into one balanced formula

- ❖ One fundamental algorithm for solving exploration-exploitation problems



The Many Forms of Exploration

- ❖ UCB is one of the best known algorithms for exploration
- ❖ Many others
 - ❖ Random walk
 - ❖ Random simulation
 - ❖ Epsilon - greedy
 - ❖ Many more...

Exploration in Modern Heuristic Search

- ❖ Doing exploration is the key difference between classic and modern heuristic search
- ❖ Many success stories
- ❖ Many different approaches to exploration
- ❖ I try to understand the common principles
- ❖ At this point, we are just doing many case studies

The Three Plus One Pillars of Modern Heuristic Search

- ❖ Three main ingredients:
 - ❖ Search (old)
 - ❖ Knowledge (old) **plus machine learning**
 - ❖ Simulations for exploration (**new**)
- ❖ All of these are used in AlphaGo
- ❖ All of these are used in many modern systems

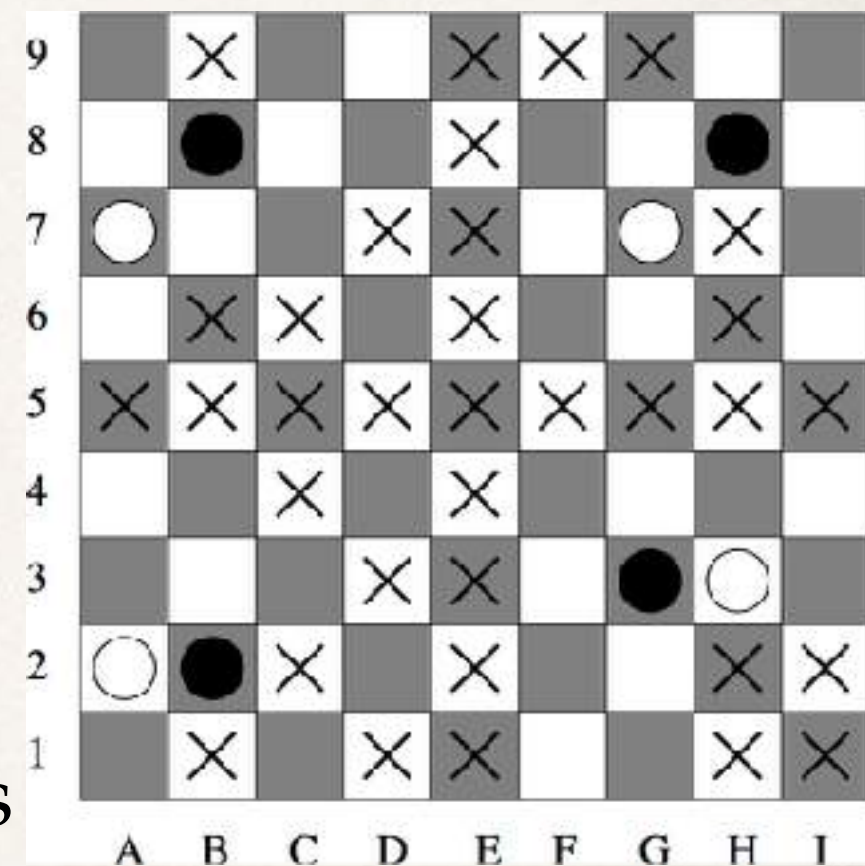
Examples of Recent Work

Game of Go

- ❖ Search = Monte Carlo Tree Search
- ❖ Knowledge, machine learning = deep convolutional neural networks
- ❖ Simulation = play full games until the end

Game of Amazons

- ❖ Modern two player game with aspects of both chess (queens) and Go (make territory)
- ❖ Search = Monte Carlo Tree Search
- ❖ Knowledge = traditional evaluation function
- ❖ Simulation = short random move sequences (about 5 moves deep) followed by evaluation
- ❖ Interesting case mixing aspects of old and new methods



Automated Planning

- ❖ Search = Greedy Best-first Search
- ❖ Knowledge = automatically constructed heuristic, specific for each problem
- ❖ Simulation = random walks, random sequences of actions
- ❖ (Much work done in my group, e.g. Arvand system)

Motion Planning

- ❖ Move robot through terrain
- ❖ RRT - rapidly exploring random tree (LaValle 1998)
- ❖ RRT* - approach optimal paths (Karaman and Frazzoli 2010)
- ❖ Extremely popular in robotics
- ❖ Early example of random walks

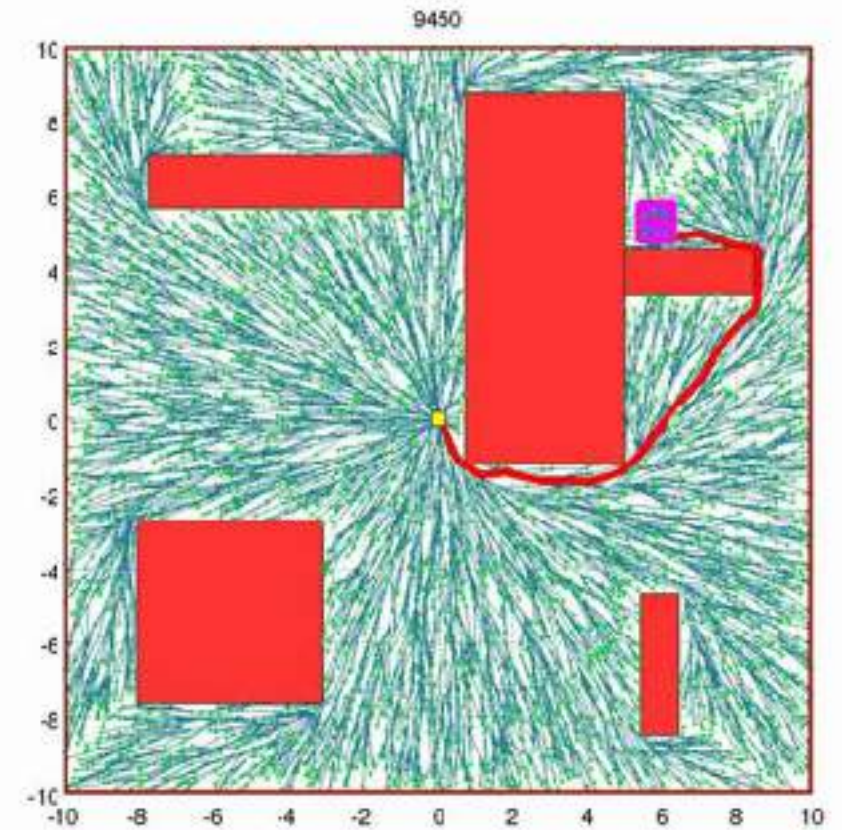


Image: Sertac Karaman

Yellow: start

Purple: goal

Red: obstacles

Green: RRT* tree

Red line: near-optimal path

Towards a General Framework

Many Results, More Questions

- ❖ Modern heuristic search has been extremely successful
 - ❖ Taking proper account of exploration makes algorithms much more robust, and able to handle harder problems
 - ❖ Advances in search allow to integrate different exploration techniques (simulations, random walks)
 - ❖ Machine learning gives much stronger domain knowledge (deep neural nets, AlphaGo)

Many More Questions

- ❖ Each success story is one data point in a larger space
- ❖ How and why exactly do these programs work?
 - ❖ We don't know
- ❖ Much development is by trial and error, not by systematic design
 - ❖ Example in Go: change program, then play thousands of test games to check it

Examples of Open Questions

- ❖ Given a new problem to solve:
- ❖ What is the right exploration method?
- ❖ Which machine learning techniques should we use?
- ❖ How do we scale to similar but harder problems?
- ❖ How do we transfer results to other problems?

Summary

- ❖ Modern heuristic search considers exploration
- ❖ Search, simulations, machine-learned knowledge
- ❖ Many diverse examples of programs which follow this pattern
- ❖ Work in progress: Looking for common ground